

# ACTUARIAL VALUATIONS

Unitrust Remainder  
Examples  
— For One Life,  
Two Lives, and  
Terms Certain

For Use in Income,  
Estate, and Gift  
Tax Purposes

## Version 3B

Table S - Based on Life Table 2000CM  
Interest at 4 Percent

Age	Annuity	Life Estate	Remainder
34	70.9197	0.14184	0.85816
35	70.5554	0.14111	0.85899
36	69.7319	0.13946	0.86054
37	68.8944	0.13779	0.86221
38	68.0495	0.13610	0.86390
39	67.1999	0.13440	0.86560
40	66.3484	0.13269	0.86731
41	65.4911	0.13098	0.86902
42	64.6326	0.12927	0.87073
43	63.7710	0.12754	0.87246
44	62.9068	0.12581	0.87419
45	62.0402	0.12408	0.87592
46	61.1718	0.12234	0.87766
47	60.3039	0.12061	0.87939
48	59.4390	0.11888	0.88112
49	58.5788	0.11716	0.88284
50	57.7242	0.11545	0.88455
51	56.8733	0.11375	0.88625
52	56.0270	0.11205	0.88795
53	55.1825	0.11036	0.88964
54	54.3378	0.10868	0.89132
55	53.4941	0.10699	0.89301
56	52.6507	0.10530	0.89470
57	51.8085	0.10361	0.89639
58	50.9598	0.10192	0.89808
59	50.1096	0.10022	0.89978
60	2559	0.09851	0.90149
61	2559	0.09680	0.90320
62	2559	0.09508	0.90492
63	2559	0.09335	0.90665
64	2559	0.10022	0.89978
65	2559	0.09851	0.90149
66	2559	0.09680	0.90320
67	2559	0.09508	0.90492
68	2559	0.09335	0.90665
69	2559	0.09163	0.90837
70	2559	0.08991	0.91010
71	2559	0.08819	0.91182
72	2559	0.08647	0.91355
73	2559	0.08475	0.91528
74	2559	0.08303	0.91701
75	2559	0.08131	0.91874
76	2559	0.07959	0.92047
77	2559	0.07787	0.92220
78	2559	0.07615	0.92393
79	2559	0.07443	0.92566
80	2559	0.07271	0.92739
81	2559	0.07099	0.92912
82	2559	0.06927	0.93085
83	2559	0.06755	0.93258
84	2559	0.06583	0.93431
85	2559	0.06411	0.93604
86	2559	0.06239	0.93777
87	2559	0.06067	0.93950
88	2559	0.05895	0.94123
89	2559	0.05723	0.94296
90	2559	0.05551	0.94469
91	2559	0.05379	0.94642
92	2559	0.05207	0.94815
93	2559	0.05035	0.94988
94	2559	0.04863	0.95161
95	2559	0.04691	0.95334
96	2559	0.04519	0.95507
97	2559	0.04347	0.95680
98	2559	0.04175	0.95853
99	2559	0.04003	0.96026



# ACTUARIAL VALUATIONS

## Version 3B

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Unitrust Remainder and Life Estate Examples  
For One Life, Two Lives, and Terms Certain

For Use in Income, Estate, and Gift Tax Purposes

Department of the Treasury  
**Internal Revenue Service**  
Publication 1458 (5-2009)  
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# ACTUARIAL TABLES ASSOCIATED WITH PUBLICATION 1458

<u>Section</u>	<u>Table</u>	<u>Type of Factors</u>
1	Table U(1)	Single Life Factors
		2-Life Last-to-Die Remainder Factors:
2-1	Table U(2)	Adjusted Payout Rates from <b>0.2 to 4.0</b> Percent
2-2		<b>4.2 to 8.0</b> Percent
2-3		<b>8.2 to 12.0</b> Percent
2-4		<b>12.2 to 16.0</b> Percent
2-5		<b>16.2 to 20.0</b> Percent
3	Table D	Term Certain Factors
4	Table F	Payout Rate Adjustment Factors
5	Table Z	Commutation Factors
6	Table 2000CM	Mortality Table

## USE OF EXAMPLES AND TABLES

This publication sets forth examples for using actuarial factors for certain income, gift, and estate tax valuations of future interests. This publication *does not contain* the tables of actuarial factors used in these examples. The actuarial tables cited in the examples below can be found on the IRS website at the following address:

**Website:** <http://www.irs.gov/retirement/article/0,,id=206601,00.html>

The examples provided are for the computation of interests in unitrusts. A unitrust is a trust wherein the trustee is directed to pay annually a fixed percentage of the fair market value of the trust computed each year, either for a life or lives or for a term of years, or for a combination of lives and years. The fixed percentage is called the payout rate. If payments are made other than annually at the beginning of each year, the payout rate must be adjusted (using Table F) in order to compute the interest involved. Some unitrusts may pay the lesser of a stated payout rate or the net trust income for the year (sometimes referred to as a Net Income Charitable Remainder Unitrust).

**Example 1** provides the method of computing the Adjusted Payout Rate given the trust's stated payout rate and the section 7520 interest rate.

**Example 2** provides the valuation of the remainder interest in a unitrust which continues until the death of a single person.

**Example 3** shows the method for computing the remainder interest following the death of the last to die of two persons.

**Example 4** illustrates the computation of the term estate interest in a unitrust which continues for a term certain.

**Example 5** shows the computation of a remainder interest following the earlier to occur of either the death of a person or the end of a term of years.

### Actuarial Tables

The factors and tables associated with this publication involving life contingencies are derived from the values of  $l_x$  taken from the Life Table for the Total Population appearing as Table 1, in "*U.S. Decennial Life Tables for 1999-2001*" published by the U.S. Department of Health and Human Services, Public Health Service, National Center for Health Statistics. That mortality table appears in the associated set of tables in Section 6, labeled as Table 2000CM.

The factors in Sections 1, 2, 3, and 5 are based on adjusted payout rates ranging from 0.2 percent to 20.0 percent in intervals of 0.2 percent.

**Table U(1)**, Section 1, contains factors for the present worth of the remainder interest in a single life unitrust.

**Table U(2)**, Section 2, contains factors for the present worth of the remainder interest in a unitrust due at the death of the last to die of two persons.

**Table D**, Section 3, contains factors for the present worth of the remainder interest in a unitrust following a term certain.

**Table F**, Section 4, contains factors for computing adjusted payout rates for annual, semiannual, quarterly, and monthly payment periods at interest rates from 0.2 percent to 20.0 percent.

**Table Z**, Section 5, contains commutation factors for the present worth of certain interests in a single life unitrust.

**Table 2000CM**, Section 6, is the underlying mortality table used to calculate factors involving life contingencies.

All of the factors associated with this publication reflect annual compounding of interest.

## Historical Synopsis of Tables

Period	Mortality Table	Interest Rate	Publications
1-1-1951 to 12-31-1970	US1938	3.5%	11
1-1-1971 to 11-30-1983	Table LN	6%	723, 723A, 723B
12-1-1983 to 4-30-1989	Table CM	10%	723C, 723D, 723E
5-1-1989 to 4-30-1989*	80CNSMT	§ 7520 rates	1457, 1458, 1459 (5-1989 release)
5-1-1999 to 4-30-2009	90CM	§ 7520 rates	1457, 1458, 1459 (7-1999 release)
5-1-2009 --	2000CM	§ 7520 rates	1457, 1458, 1459 (5-2009 release)

\* On October 22, 1988, section 7520 was enacted which prescribed the use of an interest rate equal to 120 percent of the midterm applicable federal rate, rounded to the nearest two tenths of a percent for actuarial computations.

# EXAMPLES

## A. Adjusted Payout Rate

**Example 1.** If the unitrust makes the annual distributions in the form of installments paid periodically during the year, or if the unitrust makes payments annually at a time during the year other than one year from the annual valuation date, it is necessary to adjust the payout rate to reflect the periodic installments and the period of time between the annual valuation date and the payments. This results in an “adjusted payout rate,” which is used to find the factors in the actuarial tables.

For all of the following examples, we assume that the unitrust pays out 5.0 percent per year in equal quarterly installments at the end of each quarter, and that the standard annual valuation date is the last day of the trust year, December 31. It is irrelevant if the trust is initiated and funded on another date during the year creating a short trust year, as this initial short trust year is not used to determine the period from the standard annual valuation date to the first periodic payment each year. In addition, we assume that the unitrust interest involved is to be valued at the section 7520 interest rate of 6.2 percent. Time periods are rounded to the nearest whole number of months. Based on these facts, the adjusted payout rate is 4.816 percent, determined as follows:

$$\begin{aligned} \text{Applicable Section 7520 Interest Rate} &= 6.2 \% \\ \text{Quarterly Payout Adjustment Factor} & \\ \text{Table F(6.2)} &= 0.963238 \\ \text{(First payment made at least 3 months but less than 4 months from annual valuation)} & \\ \text{Stated Annual Payout Percentage} &= 5.0 \% \\ \text{Adjusted Payout Rate} &= 5.0 \% \text{ times } 0.963238 \\ &= 4.816 \% \end{aligned}$$

## B. Single Life Remainder Interest

**Example 2.** On August 15, a person who is nearest to age 53 contributes \$1,500,000 to a charitable remainder unitrust. The trust pays to him the lesser of 5 percent per year of the annually computed value of the trust assets, or the trust net income, paid in equal quarterly installments at the end of each calendar quarter. After his death, the trust distributes the remaining corpus to a qualified charity.

Under section 7520 of the Internal Revenue Code, if a charitable contribution is allowed for a transfer of property to the trust, the taxpayer may elect to use either the section 7520 rate for the month of transfer or the rate for either of the two preceding months. We assume the taxpayer elects to use the rate for the month of transfer, 6.2 percent.

The trust pays the lesser of the stated payout rate of 5 percent or the trust net income. Under the provisions of section 1.664-4(a)(3) of the Federal Income Tax Regulations, we compute the remainder interest based on the trust's stated payout rate of 5 percent. Using the method illustrated in Example 1 above, the adjusted payout rate is found to be 4.816 percent. The required remainder factor is found by using the remainder factors found in Table U(1) for adjusted payout rates immediately above and below this adjusted payout rate, and interpolating between these factors for the remainder factor at the adjusted payout rate of 4.816 percent.

Remainder Factor, Table U(1), at 4.8 %	=	0.30453
<i>minus</i> Remainder Factor, Table U(1), at 5.0 %	=	0.29148
		-----
Difference	=	0.01305
4.816 % - 4.8 %		X
-----	=	-----
5.0 % - 4.8 %		0.01305
X	=	0.00104
Remainder Factor at 4.8 %	=	0.30453
<i>minus</i> X	=	0.00104
		-----
Required Interpolated Remainder Factor at 4.816 %	=	0.30349
<i>times</i> Initial Trust Corpus Value	=	\$1,500,000
		-----
Present Value of Remainder Interest	=	\$455,235

### C. Two Life Last-to-Die Factor

**Example 3.** On March 25, a person who is nearest to age 75 contributes \$800,000 to a charitable remainder unitrust. The trust pays to him 5 percent per year of the annually computed value of the trust assets, paid in equal quarterly installments at the end of each quarter. After his death, the trust makes the same payments to his wife (nearest to age 70) if she is then living, for such time as she survives him.

Under section 7520 of the Internal Revenue Code, if a charitable contribution is allowed for a transfer of property to the trust, the taxpayer may elect to use either the section 7520 rate for the month of transfer or the rate for either of the two preceding months. We assume the taxpayer elects to use a month for which the section 7520 rate is 6.2 percent.

Using the same method as illustrated in Example 1 above, the adjusted payout rate is 4.816 percent. The required remainder factor is found by using the remainder factors found in Table U(2) for adjusted payout rates immediately above and below this adjusted payout rate, and interpolating between these factors for the remainder factor at the adjusted payout rate of 4.816 percent.

$$\begin{array}{r}
 \text{Remainder Factor, Table U(2), at 4.8 \%} = 0.45576 \\
 \textit{minus} \text{ Remainder Factor, Table U(2), at 5.0 \%} = 0.44168 \\
 \hline
 \text{Difference} = 0.01408
 \end{array}$$

$$\begin{array}{r}
 4.816 \% - 4.8 \% \quad \quad \quad \text{X} \\
 \hline
 5.0 \% - 4.8 \% \quad \quad \quad 0.01408
 \end{array}$$

$$\text{X} = 0.00113$$

$$\begin{array}{r}
 \text{Remainder Factor at 4.8 \%} = 0.45576 \\
 \textit{minus} \text{ X} = 0.00113 \\
 \hline
 \text{Required Interpolated Remainder Factor at 5.820 \%} = 0.45463
 \end{array}$$

$$\begin{array}{r}
 \textit{times} \text{ Initial Trust Corpus Value} = \$800,000 \\
 \hline
 \text{Present Value of Remainder Interest} = \$363,704
 \end{array}$$

#### D. Trust for Term Certain

**Example 4.** On July 1, a person contributes \$5,000,000 to a charitable lead unitrust. The trustee pays to a qualified charitable organization 5 percent per year of the annually computed value of the trust assets, paid in equal quarterly installments at the end of each quarter. The trustee is to continue making these payments for 15 years. At the end of the 15 years, after all of the required charitable payments have been made, the trustee distributes the remaining trust assets to the donor.

Under section 7520 of the Internal Revenue Code, if a charitable contribution is allowed for a transfer of property to the trust, the taxpayer may elect to use either the section 7520 rate for the month of transfer or the rate for either of the two preceding months. We assume the taxpayer elects to use the rate for a month in which the section 7520 rate is 6.2 percent.

Using the same method as illustrated in Example 1 above, the adjusted payout rate is 4.816 percent. The required remainder factor is found by using the remainder factors found in Table D for adjusted payout rates immediately above and below this adjusted payout rate, and interpolating between these factors for the remainder factor at the adjusted payout rate of 4.816 percent.

$$\begin{array}{rcl}
 \text{Remainder Factor, Table D, at 4.8 \%} & = & 0.478139 \\
 \text{minus Remainder Factor, Table D, at 5.0 \%} & = & 0.463291 \\
 & & \text{-----} \\
 \text{Difference} & = & 0.014848
 \end{array}$$

$$\begin{array}{rcl}
 4.816 \% - 4.8 \% & & X \\
 \text{-----} & = & \text{-----} \\
 5.0 \% - 4.8 \% & & 0.014848
 \end{array}$$

$$X = 0.001188$$

$$\begin{array}{rcl}
 \text{Remainder Factor at 4.8 \%} & = & 0.478139 \\
 \text{minus } X & = & 0.001188 \\
 & & \text{-----} \\
 \text{Required Interpolated Remainder Factor at 4.816 \%} & = & 0.476951
 \end{array}$$

$$\begin{array}{rcl}
 \text{times Initial Trust Corpus Value} & = & \$5,000,000 \\
 & & \text{-----} \\
 \text{Present Value of Remainder Interest} & = & \$2,384,755 \\
 \\ 
 \text{Present Value of the Charitable Lead Interest} & = & \$5,000,000 - \$2,384,755 \\
 & = & \$2,615,245
 \end{array}$$

## E. Factors Involving One Life and a Term of Years

**Example 5.** On July 1<sup>st</sup>, a person transfers \$900,000 to a Grantor's Retained Unitrust which pays 5 percent per year in equal quarterly installments at the end of each quarter for 10 years or until the prior death of the grantor, who is nearest to age 60. The section 7520 interest rate for July is 6.2 percent. In order to determine the present value of the grantor's retained interest in the trust, it will be necessary to perform two computations and interpolate between the two results to get the required factor at the adjusted payout rate of 4.816 percent.

<b>First Computation:</b>	Payout Rate	=	4.8 %
	Equivalent Interest Rate Factor at 4.8 % Payout Rate	=	4.8 % / (1 - 4.8 %)
		=	0.05042
	Initial age	=	60
	<i>plus</i> Term of years	=	10
		-----	
	Terminal age		70
	${}^oU_{N_{60}}$ , Table Z (4.8)	=	55390.00
	<i>minus</i> ${}^oU_{N_{70}}$ , Table Z (4.8)	=	22203.24
		-----	
	Difference	=	33186.76
	${}^U D_x$ , Table Z (4.8)	=	4578.215
	Payout Accumulation Factor at 4.8 %	=	33186.76 / 4578.215
		=	7.24884
	<i>times</i> Equivalent Interest Rate Factor at 4.8 %	=	0.05042
		-----	
	First Payout Interest Factor, at 4.8% Payout Rate	=	0.36549

<b>Second Computation:</b>	Payout Rate	=	5.0 %
Using the same method as above, compute:			
	Second Payout Interest Factor, at 5.0 % Payout Rate	=	0.37755

Using the interpolation method shown in Example 2, interpolate between the Second Payout Interest Factor of 0.37756 and the First Payout Interest Factor of 0.36549:

<b>Required Interpolated Payout Interest Factor at 4.816 %</b>	=	0.36645
<i>times</i> Initial Trust Corpus Value	=	\$900,000
	-----	
Present Value of Grantor's Retained Interest	=	\$329,805